Please check the examination details below before entering your candidate information								
Candidate surname		Other names						
Centre Number Candidate N Cand		al GCSE						
Time 2 hours	Paper reference	4MA1/2H						
Mathematics A PAPER 2H Higher Tier		January 2022						
You must have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.								

### Instructions

- Use **black** ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided there may be more space than you need.
- Calculators may be used.
- You must **NOT** write anything on the formulae page. Anything you write on the formulae page will gain NO credit.

# Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

# Advice

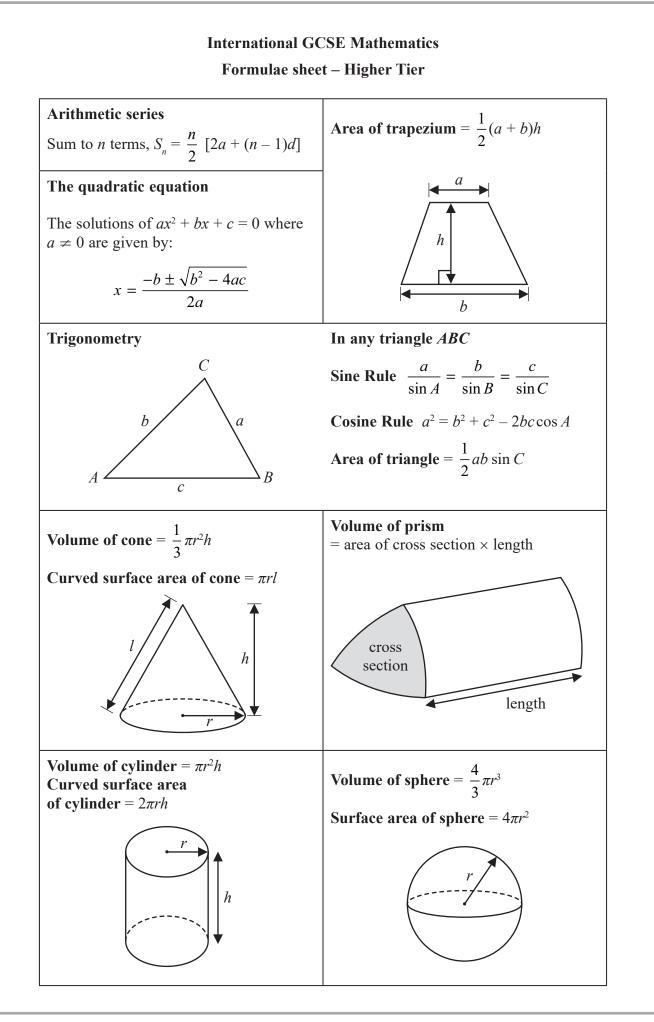
- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.





Turn over 🕨







#### Answer ALL TWENTY SIX questions.

Write your answers in the spaces provided.

You must write down all the stages in your working.

(a) Expand and simplify (y + 4)(2 - y)

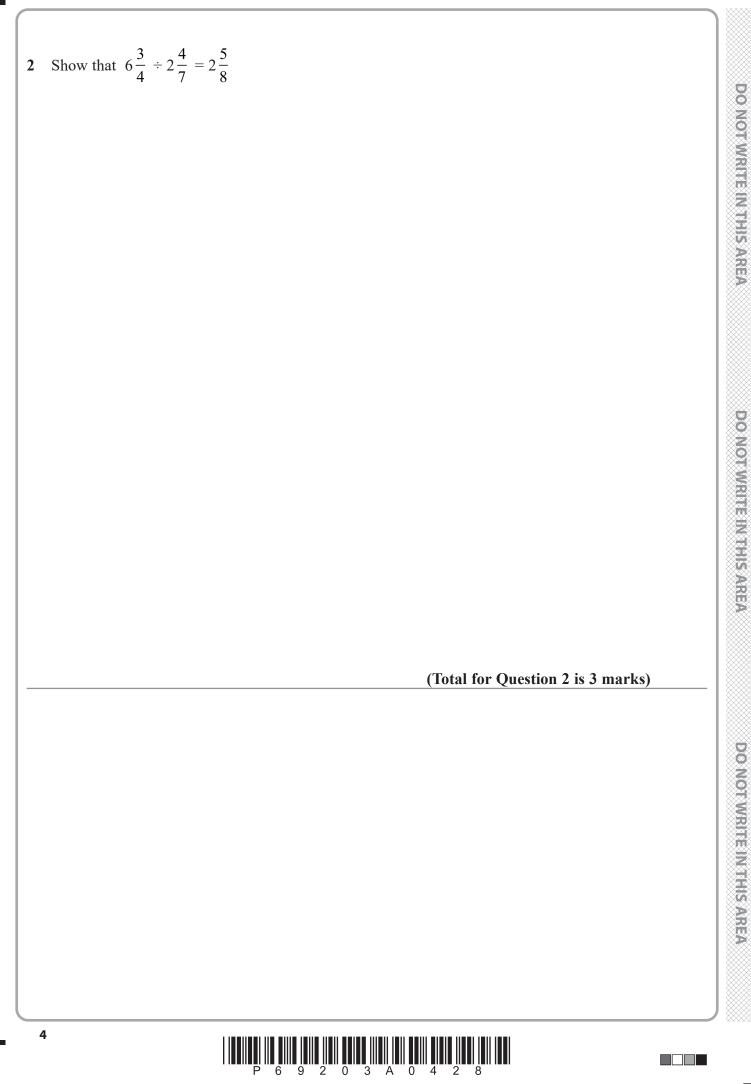
(b) Factorise fully  $15b^5c - 35b^3c^9$ 

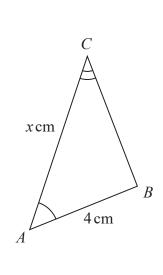
(2)

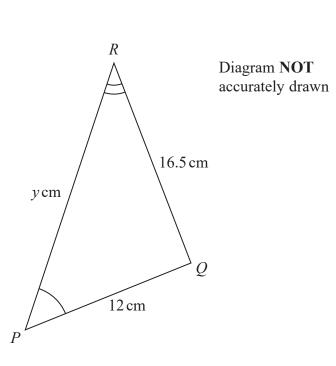
(2)

(Total for Question 1 is 4 marks)









Triangle ABC is similar to triangle PQR  $PQ = 12 \,\mathrm{cm}$  $RQ = 16.5 \,\mathrm{cm}$  $AB = 4 \,\mathrm{cm}$  $AC = x \,\mathrm{cm}$  $PR = y \,\mathrm{cm}$ (a) Calculate the length of BC

(b) Write down an expression for y in terms of x

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5

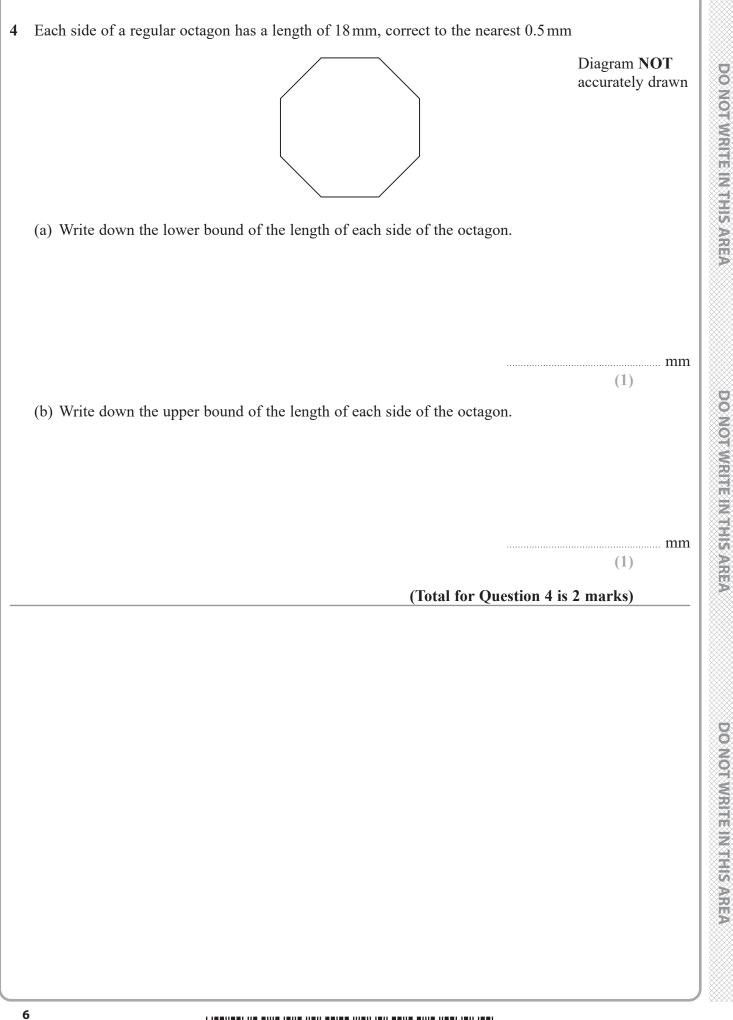
..... cm

(2)

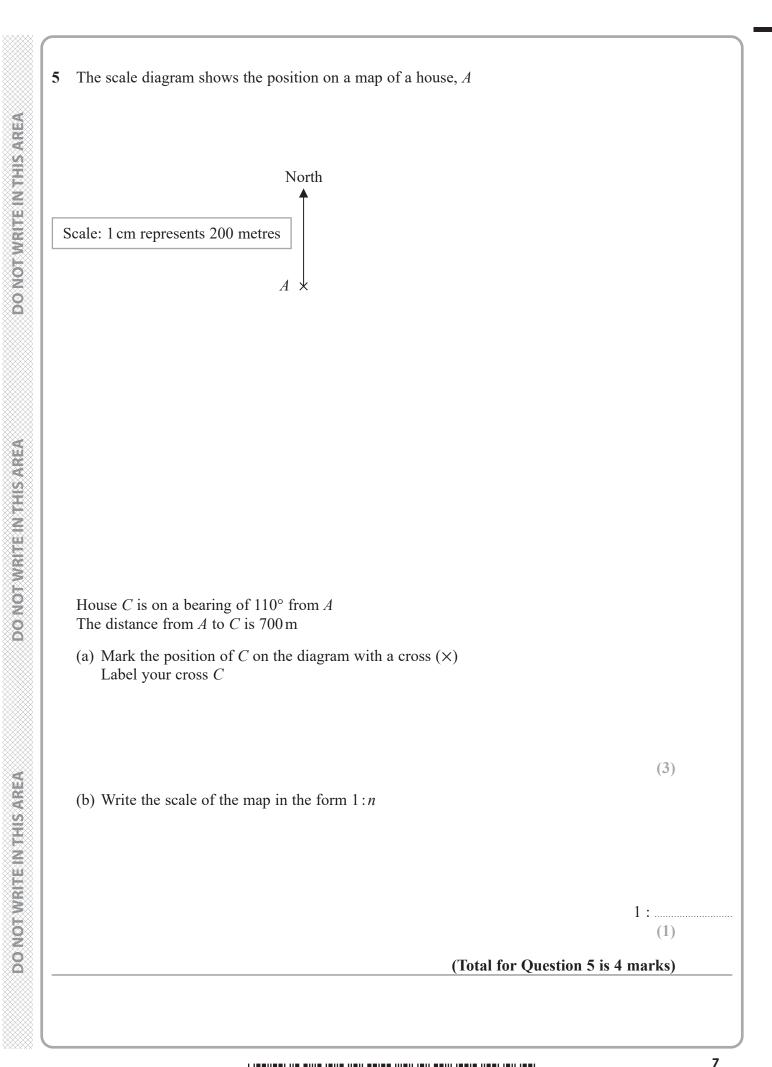
*y* = .....

(Total for Question 3 is 3 marks)

(1)



P 6 9 2 0 3 A 0 6 2 8



6 A bag contains only pink sweets, white sweets, green sweets and red sweets.

The table gives each of the probabilities that, when a sweet is taken at random from the bag, the sweet will be green or the sweet will be red.

Sweet	pink	white	green	red	
Probability			0.2	0.35	

The ratio

number of pink sweets : number of white sweets = 2:1

There are 28 red sweets in the bag.

Work out the number of white sweets in the bag.





7	Find the lowest common multiple (LCM) of 28, 42 and 63 Show your working clearly.
	(Total for Question 7 is 3 marks)
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8 The table gives information about the average house price in England in 2018 and in 2019

Year	2017	2018	2019
Average house price (£)		228314	231776

(a) Work out the percentage increase in the average house price from 2018 to 2019 Give your answer correct to one decimal place.

The average house price in 2019 was 7.7% greater than the average house price in 2017

(b) Work out the average house price in 2017 Give your answer correct to 3 significant figures.

£ .....

(3)

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(Total for Question 8 is 5 marks)



9 The frequency table gives information about the number of points scored by a player.

Number of points	Frequency					
0	13					
1	17					
2	8					
3	x					
4	11					

The mean number of points scored is 2

Work out the value of x

(Total for Question 9 is 4 marks)



11

*x* = .....

10 Solve the simultaneous equations

$$3x + 5y = 3.1$$
$$6x + 3y = 3.75$$

Show clear algebraic working.

x = ..... y = .....

(Total for Question 10 is 3 marks)



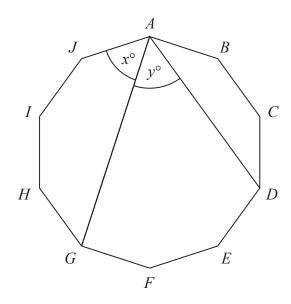


Diagram **NOT** accurately drawn

#### Show that x = y

(Total for Question 11 is 4 marks)



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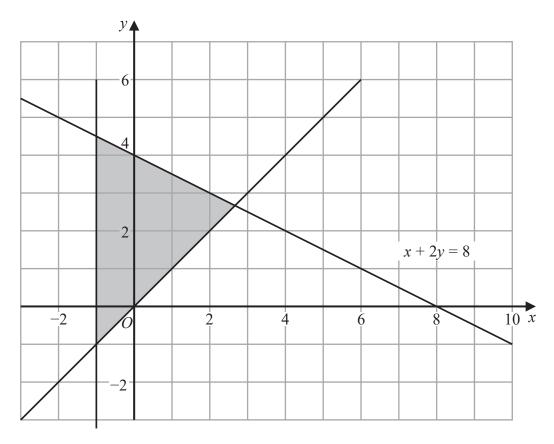
# **12** $a = 6 \times 10^{40}$

Work out the value of  $a^3$  Give your answer in standard form.

# (Total for Question 12 is 3 marks)



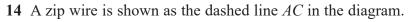
13 The shaded region in the diagram is bounded by three lines. The equation of one of the lines is given.

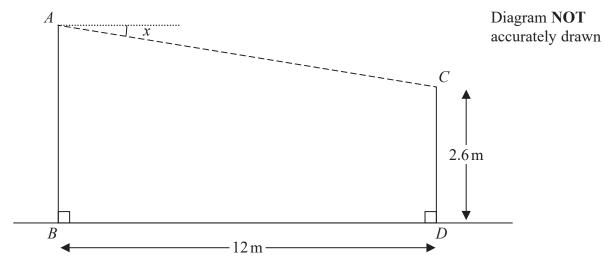


Write down three inequalities that define the shaded region.

(Total for Question 13 is 3 marks)







The zip wire is supported by two vertical posts *AB* and *CD* standing on horizontal ground.

#### $CD = 2.6 \,\mathrm{m}$ $BD = 12 \,\mathrm{m}$

The zip wire makes an angle x with the horizontal, as shown in the diagram. The design of the zip wire requires the angle x to be at least  $5^{\circ}$ 

Work out the least possible height of the post *AB* Give your answer correct to 3 significant figures.

(Total for Question 14 is 3 marks)

..... m



15	Diyar rec Here are	orded t his resu	he dista ilts.	nce, in 1	kilomet	tres, th	at he cy	cled ea	ch day	for 1	days.		
		8	10	12	13	5	23	21	7	5	16	14	
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								(10	otal fo	r Ques	stion 15	5 is 3 marks)	

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16 D, E, F and G are points on a circle, centre O

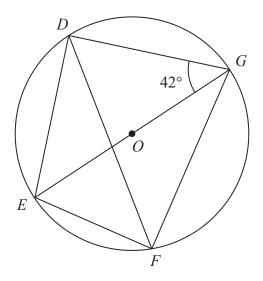


Diagram **NOT** accurately drawn

*EOG* is a diameter of the circle.

Angle  $EGD = 42^{\circ}$ 

Calculate the size of angle *DFG* Give a reason for each stage of your working.

Angle DFG =

#### (Total for Question 16 is 4 marks)

0



can be written in the form  $a + \sqrt{b}$  where a and b are integers.

(Total for Question 17 is 3 marks)



18 Prove that when the sum of the squares of any two consecutive odd numbers is divided by 8, the remainder is always 2 Show clear algebraic working.

### (Total for Question 18 is 3 marks)



19

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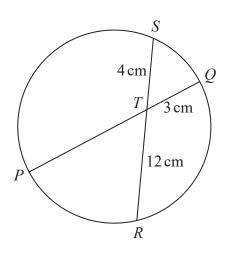


Diagram **NOT** accurately drawn

*PTQ* is a diameter of a circle. *RTS* is a chord of the circle.

TQ = 3 cm ST = 4 cm

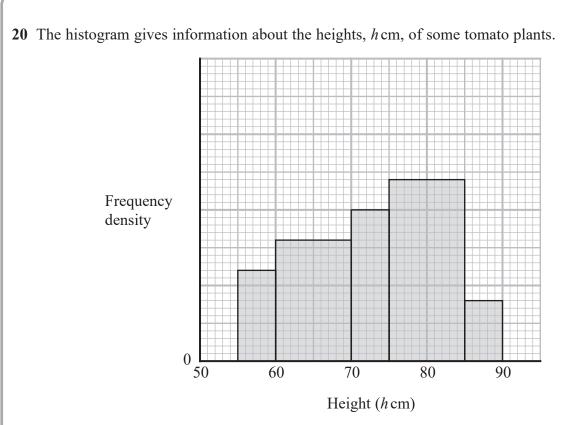
 $TR = 12 \,\mathrm{cm}$ 

Calculate the radius of the circle.

..... cm

(Total for Question 19 is 3 marks)



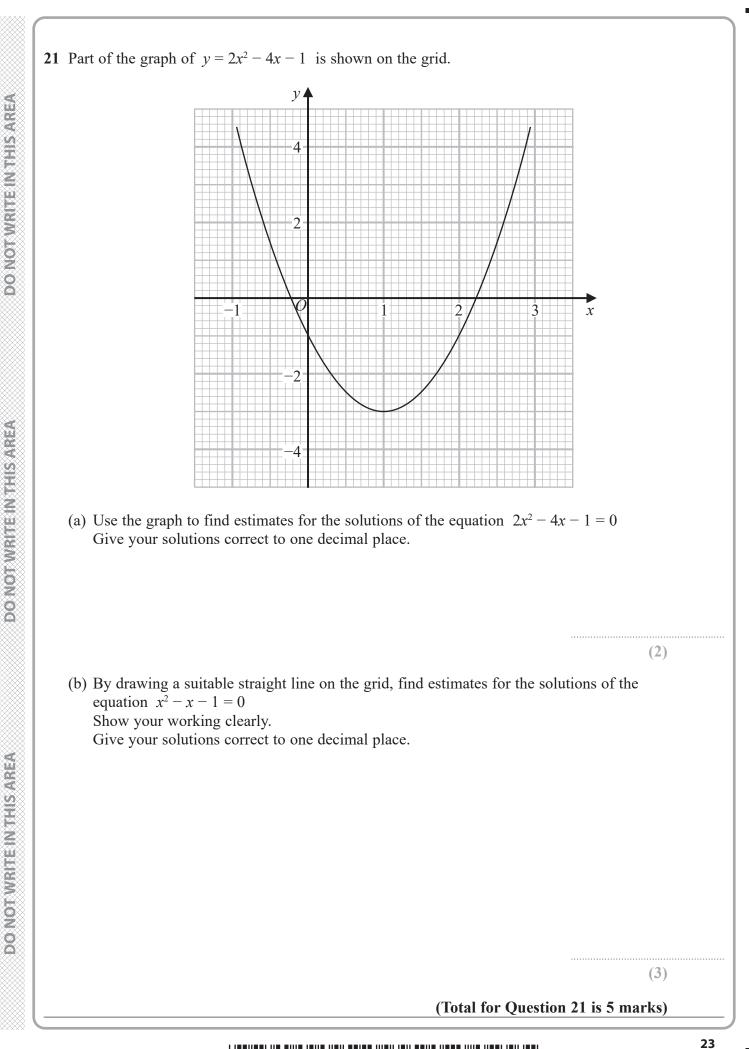


There are 12 tomato plants for which  $75 < h \le 85$ One of the tomato plants is selected at random.

Find an estimate for the probability that this tomato plant has a height greater than 82.5 cm

(Total for Question 20 is 4 marks)





P 6 9 2 0 3 A 0 2 3 2 8



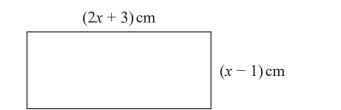


Diagram **NOT** accurately drawn

Given that the area of the rectangle is less than  $75\,\text{cm}^2$ 

find the range of possible values of x



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23 The diagram shows triangle PQR

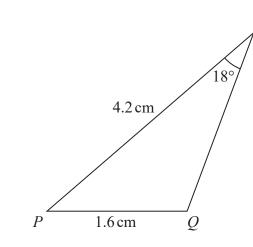


Diagram **NOT** accurately drawn

 $PQ = 1.6 \,\mathrm{cm}$   $PR = 4.2 \,\mathrm{cm}$ 

Angle  $PRQ = 18^{\circ}$ 

R

Given that angle *PQR* is obtuse,

work out the area of triangle *PQR* Give your answer correct to 3 significant figures.

 $\mathrm{cm}^2$ 

25

(Total for Question 23 is 6 marks)



**24** A particle P moves along a straight line that passes through the fixed point O

The displacement, x metres, of P from O at time t seconds, where  $t \ge 0$ , is given by

 $x = 4t^3 - 27t + 8$ 

The direction of motion of P reverses when P is at the point A on the line.

The acceleration of *P* at the instant when *P* is at *A* is  $a \text{ m/s}^2$ 

Find the value of *a* 

*a* = .....

#### (Total for Question 24 is 5 marks)

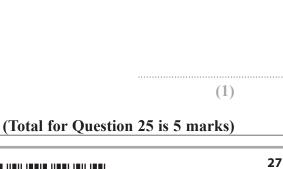


**25** The function g is defined as

$$g: x \mapsto 5 + 6x - x^2$$
 with domain  $\{x: x \ge 3\}$ 

(a) Express the inverse function  $g^{-1}$  in the form  $g^{-1}: x \mapsto \dots$ 

(b) State the domain of  $g^{-1}$ 



 $g^{-1}: x \mapsto \dots$ 



(4)

# **26** An arithmetic series has first term *a* and common difference *d*, where *d* is a prime number.

The sum of the first *n* terms of the series is  $S_n$  and

 $S_m = 39$  $S_{2m} = 320$ 

Find the value of d and the value of m Show clear algebraic working.

*d* = .....

*m* = .....

(Total for Question 26 is 5 marks)

**TOTAL FOR PAPER IS 100 MARKS** 

